РОЗВИТОК РЕГІОНІВ, ГАЛУЗЕЙ ТА ВИДІВ ЕКОНОМІЧНОЇ ДІЯЛЬНОСТІ

DEVELOPMENT OF REGIONS, INDUSTRIES AND TYPES OF ECONOMIC ACTIVITY

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THE QUALITANIVE FRACTAL ANALYSIS OF LONG TERM TIME SERIES FOR AGRICULTURAL SOILS' ELECTRICAL CONDUCTIVITY PARAMETERS: METHODS OF NONLINEAR DYNAMICS, THEORY OF CHAOS, PHASE TRAJECTORIES

The procedure of the qualitative fractal analysis of long term time series for agricultural soils' electrical conductivity parameters, for which the hypothesis of trend existence isn't confirmed, with application of the methods of nonlinear dynamics, theory of chaos and phase trajectories, is presented. The real time series characterizing mentioned above electrical conductivity parameters of Ukrainian soils is considered. The basis for similar researches is Taren's theorem. The randomness of the studied dynamical system given by time realizations is established by means of Lyapunov's indicator. The state stability is estimated by Hausdorf 's fractal dimension and the fractality index. Visual evaluation of the time series was carried out by means of the phase trajectory restoration procedure. As a result of the analysis of phase points in the phase space the split attractor is indicated, which gives the chaise to speak about its bifurcation.

Key words: qualitative fractal analysis, long term, time series, agricultural soils, electrical conductivity, parameters, methods of nonlinear dynamics, theory of chaos, phase trajectories, Lyapunov's indicator, fractal dimension, fractality index, phase space, attractor, bifurcation of an attractor.

Introduction. The system model is constructed by observed variables. In medicine, ecology, sociology the dynamics of a research object is tracked by time realizations – time series. As a rule, in the time series analysis the methods giving the quantitative forecast (point or interval) are used. For the time series, for which the hypothesis of trend existence isn't confirmed, such methods aren't productive. Application of the nonlinear dynamical system theory methods to the time series analysis is based on the hypothesis that the available series describes the behavior of the studied system, and it's the only available information about this system. According to the well-known Takens's theorem [1] a single time series suffices for an adequate description of a dynamical system as a whole.

The analysis of time series by the methods of nonlinear dynamical system theory is becoming widely applied. In terminology of this theory the process described by time series contains the deterministic chaos, or, in other words, is chaotic. From the linear analysis method point of view they are stochastic processes. The nonlinear analysis demonstrates that neither can these processes be considered as deterministic ones, nor are they absolutely random. In other words, only short-term forecasting of the system condition is possible with certain accuracy.

Today, the chaos theory remains one of the most widespread ways of forecasting and researching the dynamical system state stability. The purpose of the system stability analysis is identification of all its stationary states. If at least one of the stationary states is for any reasons threatening or undesirable, then its existence gives the chance to develop the preventive measures reducing the probability of the system transition to this state.

One of the most common forms of stability loss is the system state randomization, [1]. The mechanisms of system transition to such state are studied insufficiently. However, the fact that such state is possible requires developing new system research methods. The research tools of the chaos theory are attractors and fractals. The two prevailing dynamical system randomness criteria are Lyapunov's indicator and the fractal dimension.

Literature review. In [3] it's proved that the low information content of statistical indicators results from the fractal properties intrinsic to the behavior of time series, which empirical distribution function doesn't conform with the normal distribution. Therefore for detection of the general tendency of time series behavior it is offered to use chaos theory methods giving the chance to carry out the qualitative analysis of the studied time series at the stage of preporiate analysis. On relation to the dynamics of social and natural systems and processes the chaos theory not only explains the bifurcation phenomena (big falling or big emissions) but also claims that they can't be predicted because the nature isn't a of the repeating regularities, but is characterized by local randomness and a global order. For this reason many analysts have reasonably assumed that the fractal nature of time series will help then to recognize new regularities in the chaotic movement, [4-7].

The main formal characteristics of chaotic processes in the nonlinear dynamical system theory are the phase space and the attractor. One of the system chaotic behavior features is instability of the trajectories belonging to the attractor. Quantitatively this instability is measured by Lyapunov's characteristic indicators. Since the existence of the highest positive Lyapunov's indicator is the criterion of chaotic dynamics, the possibility of its evaluation on the basis of processing the given time series is naturally interesting.

Commonly, nonlinear dynamical systems have fractal attractors, which means that unstable phase trajectories of the systems tend to become fractals in time, [3]. On important moment of the fractal approach is the influence of the random process prehistory on the behavior of the system today. Therefore, this method of the analysis of time series is of particular interest to the researches.

As a rule, in nature real pure fractals don't exist, and it's possible to speak only about the fractal phenomena. They should be considered merely as models which are fractals approximately in statistical sense. A lot of experimental data have fractal statistics, which can be analyzed and modeled by means of fractal analysis methods, [4, 5].

One of the most popular directions of the fractal analysis is over time studying of the dynamics of such characteristic as fractal dimension. This indicator characterizes the repeatability

of statistical values of natural time series with changing scale. The fractal dimension introduced by Hausdorf and D-dimension is the main characteristic of fractal structures, [6, 7].

There are several methods of determining the fractal dimension for time series considered as a set of observable parameters of the studied dynamical system overtime. We`ll focus on two of them. First of all, it's the classical way of cellular coverage of the time series graphic representation in which the fractal dimension is defined the same way as for geometrical fractals. The second approach for studying fractal time series was offered by Benoit Mandelbrot. It's based on the researches of the English scientist Hurst and called the R/S - method.

For the majority of real time series it`s impossible to determine the fractal dimension analytically. Therefore, the V alne D are quantified, for example, through the Hurst index. In the time series analysis the influence of the present on the future can be expressed by the ratio $C = 2^{2H-1} - 1$, [8].

If a set of flat geometrical figures (cells) with the general geometrical parameters δ is considered as the time series approximation, then by Hausdorf`s definition the D – dimension is determined by the law $S(\delta) \approx \delta^{2-D}$ as $\delta \to 0$, where $S'(\delta)$ is the total area of the cells with fragmentation scale δ.

One of the time series stability indicators is the fractality index μ, [9-11]. In particular, the advantage of this index before other fractal indicators is that for computing this index with an acceptable accuracy data two orders less than for computing the Hurst indicator H suffice. It gives the chance to carry out the time series local fractal analysis based on the properties of the function $\mu(t)$.

Chaos in dynamical systems implies dynamics` evolution sensitivity to initial conditions changes. It means that two trajectories, close to each other in the phase space at some initial time point, diverge exponentially after rather small on the average time t. If d_0 is the distance between two starting points at the initial time point, then after time t distance between the trajectories leaving these points becomes $d(t) = d_0 \cdot \exp(2 \cdot \lambda \cdot t)$ or $d_n = d_0 \cdot \exp(2 \cdot \Lambda \cdot t)$ in case the system is described by different equations.

The numbers λ and Λ are called Lyapunov's indicators. Variable $d(t)$ (d_n) can`t increase infinitely because of the system limitation. It gives the opportunity to determine the measure of trajectory divergence by averaging the exponential growth on trajectory points. Then Lyapunov's indicator can be written down as:

$$\lambda = \frac{1}{(t-t_0)} \cdot \sum_{k=1}^{n} \ln\left(\frac{d(t_k)}{d(t_{k-1})} \right) \qquad (1)$$

It is possible to calculate $\lambda(\Lambda)$ in an explicit form only in some cases, such as, for instance, the case of one-dimensional displays : $X_{n+1} = f(x_n)$. When $f(x)$ is smooth and differentiable the distance between the neighboring trajectories is measured by the value $|f'(x)|$. In the case of chaos criterion it`s enough to calculate the highest Lyapunov's indicator only.

The review on Lyapunov's indicators and their usage as the movement randomness criterion is given in [2]. Here the references to the existing software products for calculation of these indicators can also be found.

One of the widespread ways of time series visual evaluation relies on the phase trajectory restoration procedure. Possibilities of such phase portrait visual analysis are very limited. However, for identification of complex non periodic time realization the phase portrait analysis gives sometimes more information than the data spectral analysis. The advantage of this approach is also that it`s applied independently of the fact whether the research object model is constructed or not. Since it`s not always possible to receive a suitable model in practice, the real way of the of the system stability analysis is the non model way of the phase trajectory behavior analysis.

The purpose of this research is the analysis of stability of the electrical conductivity parameter of agricultural soils by its time realization using the phase trajectory analysis and qualitative fractal analysis by methods.

Results and discussion. We determine the fractal dimension for time series by the classical method of cellular coverage of time series graphic image.

Let the observations of scalar equidistant time series of electrical conductivity parameter for agricultural soil be considered as $(X(t_i))_{i=1}^N$ one the interval $[0,T]$. We divide the interval into m parts by the points $O, \tau_0, \tau_1, \tau_2, ..., \tau_m, T$, where $\tau_i - \tau_{i-1} = \delta$, $\delta = \dfrac{T}{m}$, $(i = \overline{1,m})$. We denote such uniform partition of the time series $(X(t_i))_{i=1}^N$ realization interval by ω_m.

We cover the time series image with rectangles with the base δ (scale δ). It's clear, that the height of the rectangle on the interval $[\tau_i, \tau_{i-1}]$ is equal to the variation range, $A_i(\delta)$ of the time series values $x(t_i)$ on this interval. We calculate the value $V(\delta) = \sum\limits_{i=1}^m A_i(\delta)$. Then the area of such minimal coverage is $S(\delta) = V(\delta) \cdot \delta$.

By comparing this equality with Hausdorf`s $D$-dimension definition, in [q] it`s proved that $S(\delta) \approx \delta^{2-D}$ and $V(\delta) = \delta^{-\mu}$, where $\mu = D_\mu - 1$. The value D_μ is called the minimal coverage dimension, and μ is the fractality index.

When calculating the index μ in the present research the sequence of n enclosed partition ω_m, where $m = 2^n$, $n = 0,1,2,3,4,5,6$ was used. Each partition consisted of 2^n intervals containing 2^{6-n} observations $x(t_i)$. At the same time, the periods with abnormally large values $x(t_i)$ were excluded from the available realization of the time series $(X(t_i))_{i=1}^N$. The analyzed time series $(X(t_i))_{i=1}^N$ and constructed for it minimal coverage corresponding to $n = 3$ is represented in fig. 1.
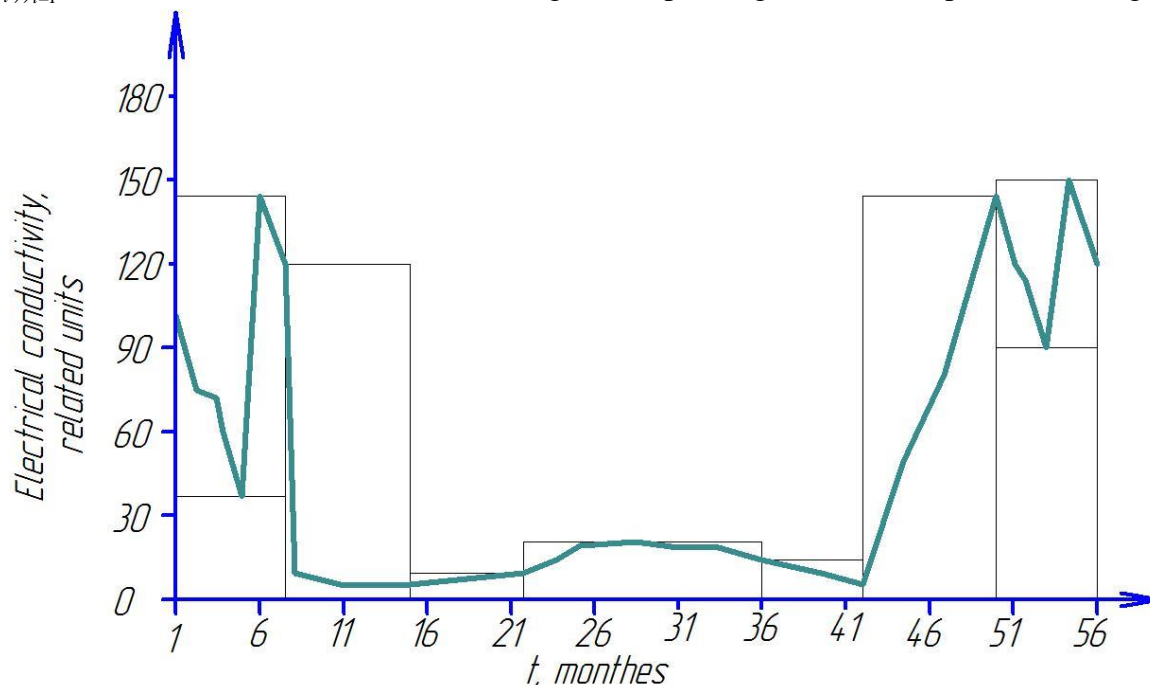

Fig. 1. Minimal cellular coverage for time series characterizing agricultural soil`s electrical conductivity

For each partition ω_m the value $V(\delta)$ was calculated. The received results of calculations are given below in Table 1.

Table 1

Value of variable V depending on partition scale δ

n	0	1	2	3	4	5	6
V	2352,6	798,8	449,5	439,4	434,6	309,9	170
Δ	1	2	3	4	8	16	32

At fig. 2 the plot of dependence $V(\delta)$ in double logarithmic scale is represented. For determination of the fractality index μ from these data by the Ordinary Least Squares method the regression line equation $y = k \cdot x + b$ was set up. Then, according to [10] $\mu = -k$.
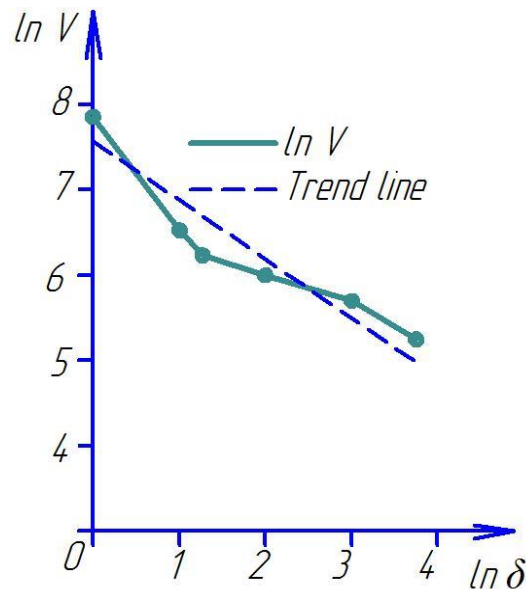
Fig 2. Dependence of the variable $V(\delta)$ in double logarithmic scale

In our case the regression equation has the form: $y = -0,66 \cdot x + 7,41$. Therefore, at the level of reliability $\alpha = 0,90$ the fractality index of the studied series is $\mu = 0,66 \cdot x \pm 0,073$.

In the present research the highest Lyapunov`s indicator $\lambda(x_1)$ was estimated by the method of comparing phase trajectory evolution points. According to this method, the value $\lambda(x_1)$ for the trajectory $x_i = x(t)$, $i = \overline{(1, N)}$ of the discrete time series $x_{i+1} = f(x_i)$ was estimated by the formula:

$$\lambda(x_1) = \lim_{N \to \infty} \left\{ \frac{1}{N} \cdot \sum_{i=1}^{N} \ln|f'(x_i)| \right\}, \tag{2}$$

corresponding to the definition of $\lambda(x_1)$ under the condition that the limit on the right-hand side exist Calculation results of the highest Lyapunov`s indicator $\lambda(x_1)$ for the time series given in fig. 1 are represented in Table 2.

The carried-out calculations have demonstrated that for the given time series $\lambda(x_1) \approx 1,18$, i.e. $\lambda(x_1) \succ 0$ therefore , the trajectory is chaotic.

Often the situation occur when one lacks the observed values for the dynamical description of an object, that is for setting its state $\bar{x}(t)$ There exit several methods for increasing the number of variables. The time delay method is the simplest and the most popular one. In case of scalar time series the consecutive values of the series $(X(t_i))_{i=1}^{N}$ separated by some interval τ (delay period) are used as the components of the state vector $\bar{x}(t)$. Thus, in the phase plane the state S_i of the research object is described by the components $\{x(t_i); x(t_i + \tau)\}$ of the time series $(X(t_i))_{i=1}^{N}$.

Table 2

Evaluation of the highest Lyapunov`s indicator $\lambda(x_1)$

N	$\sum_{i=1}^{N} \ln\left|f'(x_i)\right|$	$\lambda(x_1)$
10	4,013525	0,401353
20	3,092552	0,154628
30	21,13338	0,704446
40	39,99184	1,080860
47	55,486649	1,180567

The phase portrait allows to identity the system behavior features important from the stability point of view. To search for an attractor in the case of two (three) factors a phase space is constructed and the position of phase points is analyzed. If they are distributed uniformly, then the attractor existence hypothesis isn`t confirmed.

The phase portraits constructed for the time series shown in Fig.1 are represent in Fig 3. The value of the time delay τ is 1 year.
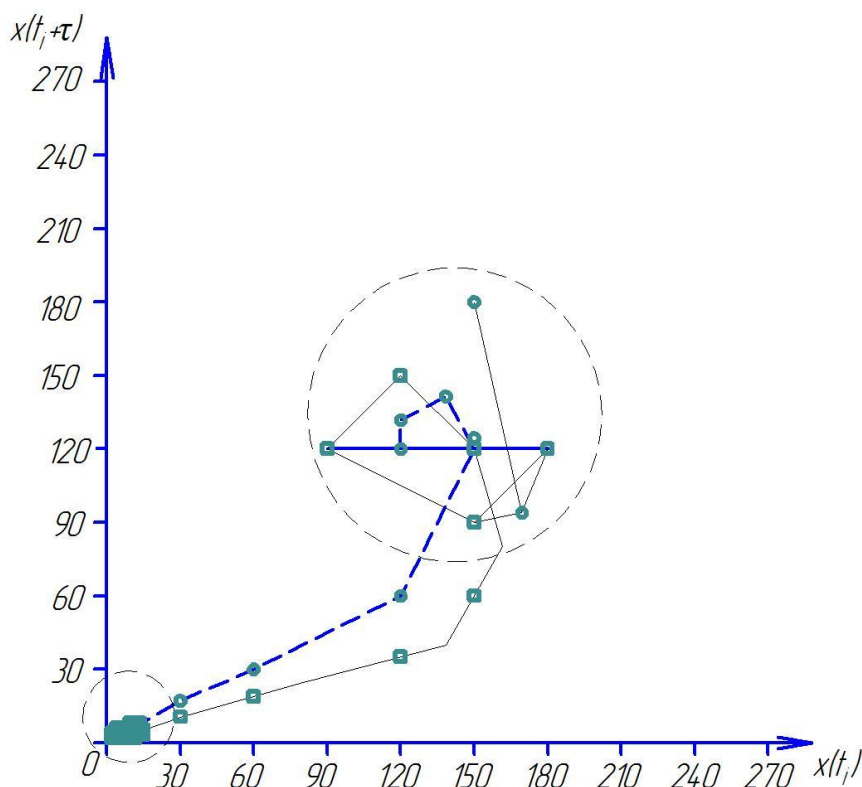

Fig. 3. Phase portraits of the time series

When fig. 3 is closely examined, it`s seen that there are two areas of phase points thickening. They can be considered as the split attractor.

In other words, attractor bifurcation takes place. Usually it`s connected with appearance in the system of such state changes which can be interpreted as spasmodic or close to them. In the electrical conductivity of agricultural soils data analysis the attractor bifurcation entails sudden crisis change of system condition with high probability.

Conclusion. The value of the highest characteristic Lyapunov's indicator $\lambda(x_1) \approx 1{,}18$ demonstrates randomness in dynamics of the studied indicator.

The computed value of the fractality index ,which is the stability indicator for the initial time series ,is $\mu = 0{,}66 \cdot x \pm 0{,}073$, i.e. $\mu \succ 0{,}5$ This value is interpreted as flat ,which indicates the

condition of relative stability for the studied process. In other words, extreme changes in the electrical conductivity parameters of agricultural soils aren't predicted in the nearest future.

The evaluation of the correlation ratio is $C = -0,88$. It implies almost complete absence of influence of the present on the future in the studied time series, which also confirms the series trendlessness hypothesis .

The analysis of the phase portraits of time series, in particular detection of the attractor bifurcation, gives reason to speak about a possible spike or spasmodic change of the electrical conductivity parameters of agricultural soils.

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ЯКІСНИЙ ФРАКТАЛЬНИЙ АНАЛІЗ ДОВГОТРИВАЛИХ ЧАСОВИХ РЯДІВ ПАРАМЕТРІВ ЕЛЕКТРОПРОВІДНОСТІ ГРУНТІВ СІЛЬСЬКОГОСПОДАРСЬКОГО

ПРИЗНАЧЕННЯ: МЕТОДИ НЕЛІНІЙНОЇ ДИНАМІКИ, ТЕОРІЇ ХАОСУ, ФАЗОВИХ ТРАЄКТОРІЙ

Проблема. *Теорія хаосу залишається одним із найпоширеніших способів прогнозування та дослідження стабільності стану динамічної системи. Мета аналізу стабільності системи - ідентифікація всіх її стаціонарних станів. Якщо хоча б одне із стаціонарних станів з будь-яких причин загрожує або небажано, то його існування дає можливість розробити профілактичні заходи, що знижують ймовірність переходу системи до цього стану. Сучасне землеробство передбачає виконання певної технологічної операції, згідно відповідної картограми-завдання, яка розробляється попередньо на основі різнопланової інформації. Знання певної структура варіабельності грунтового покриву, отриманих з використанням інформаційно-технічних систем локального оперативного моніторингу агробіологічного стану сільськогосподарських угідь, дозволяє прийняти ефективні оперативні рішення для ефективного управління агробіологічним потенціалом сільськогосподарських угідь.*

Метою *наукової статті є аналіз стійкості параметра електропровідності сільськогосподарських ґрунтів за його часовою реалізацією з використанням фазового траєкторійного аналізу та якісного фрактального аналізу різними методами.*

Результати*. Нині виникає необхідність у принципово нових підходах до ведення агропромислового виробництва, що полягає у забезпеченні належної якості виконання технологічних операцій. Якість виконання технологічних операцій є інтегральним показником ефективності виробництва сільськогосподарської продукції в межах агробіологічного поля. Необхідна якість виконання основних технологічних процесів у рослинництві забезпечується за рахунок інтегрованих інформаційно-технічних систем оперативного моніторингу агробіологічного стану сільськогосподарських угідь. У зв'язку, з цим ставиться завдання використання принципово нового класу інформаційно-технічних систем локального оперативного моніторингу агробіологічного стану сільськогосподарських угідь. Поставлене завдання досягається шляхом використання інформаційно-технічної системи оперативного моніторингу стану ґрунтового середовища конструкції для визначення електропровідних характеристик ґрунтового середовища.*

Наукова новизна*. Запропоновано процедуру якісного фрактального аналізу довготривалих часових рядів параметрів електропровідності ґрунтів сільськогосподарського призначення, для яких не підтверджується гіпотеза про наявність тренда, із застосування методу нелінійної динаміки, теорії Хаосу та фазових траєкторій. Розглянуті реальні часові ряди, що характеризують згадані параметри електропровідності українських ґрунтів (сільськогосподарського призначення). Обґрунтування для подібних досліджень є теорія Такенса. Хаотичність досліджуваної динаміки системи, що задана часовими реалізаціями, встановлена за допомогою показника Ляпунова. Оцінка стійкості стану оцінювалась фрактальною розмірністю Хаусдорфа й індексом фрактальності. Візуальна оцінка часового ряду проводилась за допомогою процедури відновлення фазових траєкторій. У результаті аналізу фазових точок фазового простору виявленні ознаки розщепленого атрактора, що дає можливість говорити про його біфуркацію.*

Висновки*. Значення найвищої характеристики показника Ляпунова демонструє випадковість у динаміці досліджуваного показника. Обчислене значення показника фрактальності, що є ознакою стійкості для початкового часового ряду, вказує на умову відносної стійкості для досліджуваного процесу. Іншими словами, екстремальних змін параметрів електропровідності сільськогосподарських ґрунтів у найближчому майбутньому не передбачається. Аналіз фазових портретів часових рядів, зокрема виявлення біфуркації атрактора, дає підстави говорити про можливий сплеск або спазматичну зміну параметрів електропровідності сільськогосподарських ґрунтів.*

Ключові слова: *якісний фрактальний аналіз, довго тривалість,часові ряди, ґрунти сільськогосподарського призначення, параметри, електропровідність, методи не лінійної динаміки, теорія Хаосу, фазові траєкторії, показник Ляпунова, фрактальна розмірність, індекс фрактальності, фазовий прості, атрактор, біфуркація атрактора.*